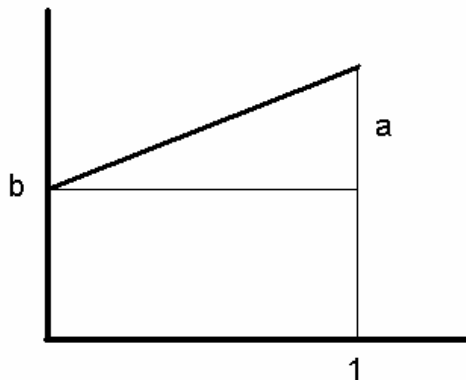


## GENERAL Documentation



Given: Values a and b.

Needed: Inverse function of area below  $f(x) = ax + b$ .

Function F for area below  $f(x)$ :  $F(x) = \frac{a}{2}x^2 + bx$

$\Leftrightarrow [a \neq 0]$

$$\frac{2}{a}F(x) = x^2 + \frac{2b}{a}x + \frac{b^2}{a^2} - \frac{b^2}{a^2} = \left(x + \frac{b}{a}\right)^2 - \frac{b^2}{a^2}$$

$\Leftrightarrow$

$$x = -\frac{b}{a} \pm \sqrt{\frac{2}{a}F(x) + \frac{b^2}{a^2}}$$

$\Leftrightarrow$

$$G(x) = -\frac{b}{a} \pm \sqrt{\frac{2}{a}x + \frac{b^2}{a^2}}$$

With  $b = w_i$  and  $a = \frac{w_{i+1} - w_i}{x_{i+1} - x_i}$  we get

$$G(x) = -\frac{w_i(x_{i+1} - x_i)}{w_{i+1} - w_i} \pm \sqrt{\frac{2(x_{i+1} - x_i)}{w_{i+1} - w_i}x + \left(\frac{w_i(x_{i+1} - x_i)}{w_{i+1} - w_i}\right)^2}$$